

# CANTT ACADEMY

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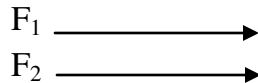
## CHAPTER: 4 Turning Effect of Force

### Parallel Force:-

Such forces in which point of action are different but line of action are parallel to each other are called parallel force.

### Like Parallel Forces:-

Those parallel forces (in which) direction is same are called like parallel force.



### Un like Parallel Force:-

A resultant force is a single force that has the same effect as the combined effect of all the forces to be added.

### Addition of Forces:-

Force is a vector quantity it has magnitude as well as direction. Therefore different forces cannot be added by ordinary method.

A special method is used to add vector quantities. This method is called “Head to tail rule”

### Head to tail Rule:-

According to head to tail rule first of all we will select a suitable scale then we will draw the vectors of all forces according to this scale.

Suppose we have tow vectors A and B and we want to add vector B in to vector A. For this purpose we will draw these two vectors in such a way that head of vector A joins with tail of vector B then we will join tail of vector B with head of Vector A.

A line which joins tail of vector A with head of vector B is called resultant vector.

### Rectangular Components:-

Those component of a force which are mutually perpendicular to each other are called rectangular component.

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## Explanation:-

Consider a force 'F' represented by a line OA making an angle with x-axis. Draw a perpendicular AB from point 'A' on x-axis.

According to head to tail rule OA is the resultant of

OB and BA

$$OA = OB + BA$$

The component OB and BA are perpendicular to each other so they are called rectangular components of vector OA since the component OB is along x-axis so it is called x-component of the force F and it is represented by  $F_x$ .

Since the component BA is along y axis so it is called y-component of vector F and it is represented by  $F_y$

Now from eq (1)

$$OA = OB + BA$$

$$F = F_x + F_y$$

The magnitude of  $F_x$  and  $F_y$  can be found by using trigonometric ratios.

In right angle triangle OA is

We know

$$\sin \theta = \frac{P}{H}$$

$$\sin \theta = \frac{F_y}{F}$$

$$F \sin \theta = F_y$$

$$F_y = F \sin \theta (-)$$

$$F_y = F \sin \theta (-)$$

Now

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$$\begin{aligned}\cos \theta &= \frac{B}{H} \\ \cos \theta &= \frac{F_x}{F} \\ \cos \theta &= \frac{F_x}{F} \\ F_x &= F \cos \theta\end{aligned}$$

|                       |
|-----------------------|
| $F_x = F \cos \theta$ |
|-----------------------|

## Determination of a Force from the perpendicular components:-

By using rectangular components we can find magnitude of resultant force

Using Pythagoras theorem

$$\begin{aligned}(H) &\neq (B)^2 + (F)^2 \\ (H) &\neq (F_x)^2 + (F_y)^2\end{aligned}$$

Taking square root

$$\sqrt{(H)^2} = \sqrt{(F_x)^2 + (F_y)^2}$$

$$H = \sqrt{(F_x)^2 + (F_y)^2}$$

$$H = \sqrt{(F_x)^2 + (F_y)^2}$$

## Direction of resultant force:-

We know

$$\tan \theta = \frac{P}{B}$$

$$\tan \theta = \frac{F_y}{F_x}$$

$$\tan \theta = \tan^{-1} \left( \frac{F_y}{F_x} \right)$$

|   |
|---|
| $\theta = \tan^{-1} \left( \frac{F_y}{F_x} \right)$ |
|---|

## Rigid Body:-

A body is composed of large number of small particles if the distance between all pair of particles does not change by applying forces then it is called a rigid body.

**OR**

Such a body which retains its shape and size by applying a force is called a rigid body.

## Axis of Rotation:-

A line around which a body moves or rotates is called axis of rotation.

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## Torque or Moment of Force:-

The turning effect of a force is called torque or moment of force. Mathematically it is defined as “The product of force and moment arm is called torque”.

## Formula:-

$$\text{Torque} = (\text{moment arm}) (\text{force})$$
$$T = r \times F$$

## Quantity:-

Torque is a vector quantity.

## Dependence of Torque:-

Torque depends upon two factors.

1. Force
2. Moment arm

## Moment Arm:-

Moment arm is the perpendicular distance from point of action of force to point of rotation.

## Clock Wise Torque:-

If the rotation produced in a body is in clock wise direction then the torque produced in the body is called clock wise torque.

## Anti Clock Wise Torque:-

If the rotation produced in a body is in anti clock wise direction then the torque produced in the body is called anti clock wise torque.

## Principle of Momentum:-

If the sum of clock wise torque is equal to the sum of anti clock wise torque then a body is balanced and it is called principle of moments.

## Center of Mass:-

Centre of mass of a mass of a system is such a point where an applied force causes the system to move without rotation.

## Centre of Gravity:-

A point where whole weight of the body appears to act vertically downward is called centre of the gravity of the body.

## Couple:-

A couple is formed by two parallel forces of the same magnitude but not along the same line.

**OR**

When two equal, opposite and parallel forces act at two different points of the same body then they form a couple.

## Example:-

1. While driving a car the forces applied on steering wheel of the car forms a couple.

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2. To open or close a water tap a couple is applied.

## Equilibrium:-

A body is said to be in equilibrium. If no net force acts on it.

If a body is in equilibrium then it means that this body is at rest or moving with uniform velocity.

## Condition of Equilibrium:-

There are two conditions of equilibrium.

1. First condition of equilibrium.
2. Second condition of equilibrium.

### 1. First Condition of Equilibrium:-

According to first condition of equilibrium if the resultant of all the forces acting on a body is zero then the body is in equilibrium

$$F_1 + F_2 + F_3 + F_4 + \dots + F_n = 0$$

$$\Sigma F = 0$$

Here  $\Sigma$  (sigma) is a greek letter and it is used to find sum.

According to first condition of equilibrium the sum of all the forces acting along x-axis must be zero and the sum of all the forces acting along y-axis must be zero.

$$\Sigma f_x = 0$$

And

$$\Sigma f_y = 0$$

### 2. Second Condition of Equilibrium:-

According to second condition of equilibrium the resultant torque of all the forces acting on a body must be zero.

$$\Sigma \tau = 0$$

## States of Equilibrium:-

There are three states of equilibrium.

1. Stable equilibrium
2. Unstable equilibrium

### 1. Stable Equilibrium:-

A body is said to be in stable equilibrium. If it returns to its previous position after a slight tilt.

### 2. Un-Stable Equilibrium:-

If a body does not return's to its previous position after a slight tilt then this state of equilibrium is called unstable equilibrium.

### 3. Neutral Equilibrium:-

If a body remains in its new position when it is disturb from its previous then this state of equilibrium is called neutral equilibrium.